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# FISHERIES DIVISION

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#### **Evaluation of Michigan Creel Survey Catch Rate Estimator**

**Roger N. Lockwood** 

Michigan Department of Natural Resources Institute for Fisheries Research 212 Museums Annex Building Ann Arbor, Michigan 48109-1084

Abstract.-Access-site creel surveys are conducted at numerous Great Lakes ports and on inland waters each year in Michigan to estimate angling effort and catch. Estimated catch is the product of estimated angler hours and catch rate. Catch rate has been determined by averaging angler party catch per hour by species, angling mode, and time period. This method for calculating catch rate is not weighted by number of anglers in the party or by length of fishing trip which could lead to biases in estimates. Effects of bias on accuracy and precision of catch per hour estimates were measured using Monte Carlo sampling techniques on 132 data sets from Michigan access-site creel surveys. Each data set was considered a discrete population and population catch rate parameters were compared with sample catch rate estimates. Estimated mean catch rate by angler party was significantly greater,  $P_{\mu} \leq 0.05$ , than population catch rate parameters in 82 data sets and significantly less in 49 others. Due to trip length and angler party size bias, the sample confidence limits were incorrectly represented in 123 of 132 data sets. Biases associated with averaging angling party catch rates were found to be prevalent in Michigan access-site creel surveys. I concluded that averaging angler party catch rates is inappropriate for Michigan access-site creel surveys. Calculating catch rate by dividing total catch by total hours from angler interviews eliminates the bias.

#### Introduction

Michigan Department of Natural Resources (MDNR), Fisheries Division conducts creel surveys on inland and Great Lakes waters of Michigan to evaluate status and trends in fish populations, changes in sportfishing regulations, trends in angling effort, success of fish plantings, and success of other management practices (Ryckman and Lockwood 1985; Rakoczy and Lockwood 1988; Alexander et al 1979; Schneider and Lockwood 1979; Beyerle 1984; and Galbraith and Schneider 1984). In 1994, some 16,000 angling parties fishing Lake Michigan (G. Rakoczy, MDNR, personal communication) and

over 2,000 angling parties fishing six inland lakes and Southern Michigan's Rogue River (Lockwood 1995) were interviewed.

Michigan creel surveys are best described as access-site creel surveys (Malvestuto 1983) and follow a stratified design using structured random sampling within strata (Fabrizio et al 1991). These access-site creel surveys consist of two separate sampling components, angler counts and angler party interviews. Angler counts are made at each site or lake and averaged by angling mode and time period (Ryckman 1981; Ryckman and Lockwood 1985). Mean counts are then expanded by hours sampled in a given time period to estimate total angling effort. Angling parties are interviewed as they leave a site (completed trip interview) or prior to leaving while they are still actively fishing (incompleted trip interview). Individual creel surveys consist of mostly, or entirely, completed trip interviews or incompleted trip interviews. For example, all Great Lakes interviews collected in 1994 were completed trip interviews (G. Rakoczy, MDNR, personal communication) as were all 1994 inland lake interviews. The 1994 Rogue River survey was comprised primarily of incompleted trip interviews (85%).

Angler success is estimated by catch rates which are determined from interviews. Several methods exist for calculating catch rates. Crone and Malvestuto (1991) assessed five methods for calculating catch rates and report that substantial differences in catch rate estimates existed between methods as did variability (determined by the coefficient of variation) associated with each method. For Michigan creel surveys, catch rate for each species (i) is calculated as a mean of ratios  $(\overline{R}_i)$ :

$$\overline{R}_{i} = \frac{\sum_{j=1}^{n} \left(\frac{c_{i,j}}{h_{j}}\right)}{n},$$
(1)

where

i = species, c = total catch of angler party j, h = total hours fished by angler party j, n = total angler parties interviewed.

Pollock et al. (1994) recommends using this estimator with incomplete trip interviews recorded by individual angler. Mean-of-ratios estimator can be correctly used when there is no bias due to angler trip length or angler party size (Hayne 1991), and averaging daily catch rates over many days is appropriate for calculating mean daily catch rates (Malvestuto 1983). Jones et al. (1995) showed effects of trip length bias on the mean-of-ratios estimator, and its variance, using a creel survey of summer flounder *Paralichthys dentatus* anglers in Virginia. Bias concerns allied with using the mean-of-ratios estimator for completed trip interviews have also been noted by Jessen (1956) and Hayne (1991).

Neuhold and Lu (1957), Malvestuto (1983), Hayne (1991) and Pollock et al. (1994) recommend a ratio-of-means ( $\hat{R}_i$ ) estimator with completed trip interviews:

$$\hat{R}_{i} = \frac{\sum_{j=1}^{n} c_{i,j} / n}{\sum_{j=1}^{n} h_{j} / n},$$
(2)

where

i = species, c = catch of angler party j, h = total hours fished by angler party j, n = total number of interview records.

Ryckman (1983) utilized angler count and interview data sets from several Michigan creel surveys in an attempt to predict sampling levels necessary to minimize bias and maximize precision of estimated angling pressure and catch per hour (CPH). Sample CPH was calculated using the mean-of-ratios estimator,  $\overline{R}_i$  in (1), and was compared with total catch per hour of the data set,  $R_{i}$  in (2). That study indicated that while precision of sample CPH improved with increased sampling, biases existed in particular data sets which showed no apparent trend nor magnitude in relation to sample CPH, estimates or sample size. Sample CPH, was lower (negative bias) than total CPH in some data sets and greater (positive bias) in others. Also, sign and magnitude of sample CPH, bias that existed at low levels of sampling (e.g., 20% of the population) remained when sampling was increased to as much as 90% of the population.

I selected 132 data sets from Michigan creel surveys to further evaluate catch rate biases associated with a mean-of-ratios estimator and determine if a ratio-of-means estimator is more appropriate for use in Michigan. Variability of these data sets was also evaluated to ascertain appropriate sampling levels for future Michigan creel surveys.

#### Methods

#### Selection of Data Sets

Interview data sets were chosen for analysis which represented five modes of angling and 13 species of freshwater fish (Table 1). These data sets were assumed to characterize the diverse sport fisheries that exist in Michigan and to replicate fishery types (Great Lakes or inland, angling mode, and species harvested). Individual data sets contained 50-1,148 interview records and only completed trip interviews were analyzed. Interviews portrayed catch by angling party and party size varied from 1-6 anglers. None of the interviews were originally collected for use in this study, but were gathered in conjunction with independent management or research projects. Catch by species in each instance was harvest by species; no catch-and-release data were included.

#### Sampling Techniques

Each of the selected data sets was treated as a finite population to be sampled. Monte Carlo sampling techniques were used to sub-sample the data sets and then calculate estimates. Sampling levels (k) for each data set were 1-10% (at 1% intervals), 15%, 20%, 30%, 50%, 70% and 90% of the available records. Extra sampling was done at lower levels since most surveys sample <20% of the anglers (Ryckman 1983). Greater sampling levels (>20%) were done since it was assumed that as a greater proportion of a population is sampled, the more likely the sample estimate is to correctly represent the population parameter. Each sampling level was replicated 500 times and records were randomly selected without replacement for each replication.

#### Catch Rate Estimators

For each data set the true catch per hour ( $\Theta$ ) was calculated using equation (2) and all interview records in a data set. This is considered the correct measure of catch per hour by species because in a true census:

$$C_{i} = \frac{\sum_{j=1}^{P} C_{i,j}}{\sum_{j=1}^{P} H_{j}} \bullet \sum_{j=1}^{P} H_{j}, \qquad (3)$$

where

- i = species,
- C = total catch of species i by angler party j,
- H = total hours fished by angler party j,
- P = number of angler parties in population,

accurately determines total catch. The goal of Michigan creel surveys is to accurately estimate  $C_i$ .

Mean-of-ratios ( $\overline{R}_i$ ) and ratio-of-means ( $\hat{R}_i$ ) catch rates were calculated, by species for each replication and sampling level (k). Estimate of  $\overline{\overline{R}}_{ik}$  then was:

$$\overline{\overline{R}}_{i,k} = \frac{\sum_{j=1}^{N} \overline{R}_{i,k,j}}{N}, \qquad (4)$$

where

i = species, k = sampling level,  $\overline{R}$  = mean of ratios for replication j, N = number of replications.

The variance of the  $\overline{\overline{R}}_{i,k}$ ,  $(\hat{\operatorname{var}}(\overline{\overline{R}})_{i,k})$ , was calculated as:

$$\operatorname{var}\left(\overline{\overline{R}}\right)_{i,k} = \frac{\sum_{j=1}^{N} \left(\overline{R}_{i,k,j} - \Theta_{i}\right)^{2}}{N(N-1)}, \quad (5)$$

where

i = species,

- k = sampling level,
- $\overline{R}$  = mean of ratios for replication j,
- $\Theta$  = data set catch per hour of species i, in equation (2),
- N = number of replications.

Estimate of  $\hat{R}_{i,k}$  then was:

$$\overline{\hat{R}}_{i,k} = \frac{\sum_{j=1}^{N} \hat{R}_{i,k,j}}{N}, \qquad (6)$$

where

i = species, k = sampling level,  $\hat{R}$  = ratio of means for replication j, N = number of replications.

The variance of  $\overline{\hat{R}}_{i,k}$ ,  $(\hat{var}(\overline{\hat{R}})_{i,k})$ , was calculated as:

$$\operatorname{var}\left(\overline{\hat{R}}\right)_{i,k} = \frac{\sum_{j=1}^{N} \left(\widehat{R}_{i,k,j} - \Theta_{i}\right)^{2}}{N(N-1)}, \quad (7)$$

where

i = species, k = sampling level,  $\hat{R}$  = ratio of mean for replication j,  $\Theta$  = data set catch per hour of species i, in equation (2), N = number of replications.

Variance formulas (5) and (7) are derived from Hammersley and Handscomb (1964) and Hall (1992), and represent the total variation associated with estimated  $\hat{\Theta}$  (either  $\overline{\overline{R}}$  or  $\overline{\hat{R}}$ ):

$$v\hat{a}r(\hat{\Theta}) = S^2\hat{\Theta} + (Bias\hat{\Theta})^2, \qquad (8)$$

where

 $S^2 \hat{\Theta}$  = variation due to sampling,  $Bias \hat{\Theta}$  = estimated bias.

#### Statistical Tests

Estimates of catch rate and 95% confidence limits at the 90% sampling level for each estimator  $(\overline{R_i} \text{ and } \overline{R_i})$  were compared to actual catch per hour  $(\Theta_i)$ . With 90% of a given population sampled, error due to sampling is minimized and biases associated with an estimator are readily apparent. Differences were considered significant when  $\Theta_i$  fell outside the 95% confidence limits for a particular estimator (Hammersley and Handscomb 1964). Bias was measured as the difference between  $\Theta_i$  and the 90% sampling level catch rate mean for  $\overline{R_i}$  or  $\overline{R_i}$ . Bias was calculated for each data set and influence of bias on estimated confidence limits for a given data set was calculated as:

$$\frac{\hat{B}_i}{\hat{\sigma}_i},\tag{9}$$

where

 $\hat{B}_i$  = bias associated with estimator  $\overline{\overline{R}_i}$  or  $\overline{\hat{R}_i}$ ,  $\hat{\sigma}_i$  = estimated standard deviation from  $\hat{var}(\overline{\overline{R}})_i$  or  $\hat{var}(\overline{\hat{R}})_i$ .

Confidence limits were considered misrepresented when  $\hat{B}_i / \hat{\sigma}_i > 0.20$  (Cochran 1977).

Stepwise linear regression was used to measure influence of angler party size and length of fishing trip on individual angler party catch rate in each data set. Variables were considered significant and included in regression equations at  $P_{\alpha} = 0.05$ . Regression analysis was done using SPSS for Windows (Version 6.0, SPSS Inc., 1993).

Multiple regression analysis was used to evaluate sampling levels (number of party interviews sampled) for future access-site creel surveys. Number of angler party interviews from the Monte Carlo simulation was regressed on coefficient of variation (CV) expressed as a percentage (Fowler and Cohen 1990) and  $\overline{\hat{R}}_i$ .

#### Results

#### Monte Carlo Sampling

Replications were varied from 2-500 on a sample data set to determine appropriate number of replications (Figures 1 and 2). Bias and CV associated with each estimator stabilized at 50 replications and remained similar out to 500 replications. As a result, 500 iterations was considered satisfactory for each Monte Carlo simulation.

#### Mean of Ratios

 $[\overline{R}_i]$ Mean-of-ratios estimator was significantly different from actual catch per hour  $[\Theta_i]$  in 131 of the 132 comparisons (Tables 2-14).  $\overline{R}_i$  over estimated  $\Theta_i$  for 82 data sets and under estimated  $\Theta_i$  for 49 others. Only for a walleye pier fishery at Holland on Lake Michigan was  $\overline{R}_i$ not significantly different from  $\Theta_i$  (Table 13).  $\overline{R}_i$  under or over estimated  $\Theta_i$  by  $\geq 20\%$  on 67 occasions;  $\geq$ 30% on 44 occasions;  $\geq$ 40% on 30 occasions; and  $\geq$ 50% on 21 occasions (Figure 3). Confidence limits associated with this method were misrepresented for 123 of 132 data sets. Bias was quite variable and under or over estimated  $\Theta_i$ by 0.36-285.50%.

Length of fishing trip was a significant factor affecting  $\overline{R}_i$  in 33 data sets (Tables 15 and 16). Of these 33, catch rate declined as length of fishing trip increased for 7 data sets and increased as length of fishing trip increased for 26 data sets. Similarly, number of anglers in a fishing party significantly affected  $\overline{R}_i$  in 24 data sets. Catch rate declined as number of anglers in a fishing party increased for 23 data sets, and increased as number of anglers in a party increased for only one data set.

#### Ratio of Means

Estimator  $\overline{\hat{R}}_i$  was significantly different from  $\Theta_i$  in only 1 of the 132 comparisons (Table 4). Bias was insignificant and  $\overline{\hat{R}}_i$  under estimated  $\Theta_i$  by 0.71% in that one instance. In 59 comparisons,  $\overline{\hat{R}}_i$  was identical to  $\Theta_i$  and maximum deviation of  $\overline{\hat{R}}_i$  was an over-estimation of 3.33%. Confidence limits were never misrepresented.

#### Estimation of Sampling Levels

As a result of analyzing bias, only sampling levels for catch rate estimator  $\overline{\hat{R}}_i$  were considered.  $\overline{\hat{R}}_i$  in the 132 data sets analyzed ranged from 0.0003-4.3892. Monte Carlo sampling of the original 132 data sets resulted in the creation of 2,112  $\overline{\hat{R}}_{i,k}$  and  $v\hat{a}r(\overline{\hat{R}})_{i,k}$  values. A data base was developed containing these estimates. Each record in the data base included  $\overline{\hat{R}}_{i,k}$ ,  $CV_{i,k}$  (based on  $v\hat{a}r(\overline{\hat{R}})_{i,k}$ ) and the number of angler parties, which ranged from 1-1,033, sampled at level k.

A natural log-linear multiple regression model was developed to evaluate sampling intensities of the 2,112 Monte Carlo records (Figure 4). Transformation of sample size (number of angler party interviews) was regressed on transformations of  $CV_{ik}$  and  $\hat{R}_{i,k}$ . Variation in regression coefficients accounted for 83% of the variation (R=0.91) in number of angler party interviews and was significant at  $P_q \leq 0.01$ . As catch rate increased and CV declined, sampling levels were reduced (Figure 4). Sampling levels at a given CV are quite similar when  $\hat{R} \ge 0.07$ . However, when  $\hat{R}$  <0.07 substantially more interviews are required to achieve similar precision. CV of 20%, when  $\hat{R} = 0.07$ , is attainable with 98 angler party interviews and attainable with 78 angler party interviews when  $\hat{R} = 0.13$ . When  $\hat{R} = 0.01$ , however, 200 interviews are needed for a CV=20%.

#### Discussion

Fisheries Division, of the then Michigan Conservation Department, began conducting creel surveys in 1927 (Tait 1953). These first surveys were true censuses, that is all anglers fishing on a particular lake were counted and interviewed. Partial censuses were conducted during following years, however they were not conducted using any specific survey design. By the early 1950s, sampling designs were incorporated and Tait (1953) conducted the first evaluation of Michigan's creel survey methods. Several conclusions were drawn from Tait's study and help to explain reliance on mean-of-ratios estimator used in Michigan to date.

Only two sources of catch-per-hour bias were recognized in Tait's (1953) evaluation. First. methods for developing a sampling schedule may be biased, and second, a creel clerk might not randomly select angling parties to interview. Also, catch rate by individual angler was assumed to be equal to catch rate of angling parties. Both ratio of means and mean of ratios estimators were given as alternatives for calculating catch rate. Mean-ofratios estimator was selected for use in Michigan creel surveys rather than ratio-of-means estimator for two reasons. First, a method or methods for calculating variance of ratio of means was unknown. Second, it was known that distribution of catch rates by anglers is highly skewed and mean-of-ratios estimator tended to normalize this distribution.

Potential bias problems associated with meanof-ratios estimator were inadvertently suggested by Tait (1953). Due to intense sampling effort of some of these early creel surveys, Tait (1953) was able to compare taking mean-of-ratios catch rate for a season with mean-of-ratios catch rate for each hour sampled. Individual hourly catch rates were weighted by that hour's angling pressure. Resulting catch rates from these two methods differed by 3.0-20.8%. My evaluation of catch rate for the duration of an angling trip would compensate for the length of trip bias.

Bias concerns associated with averaging angler or angler party catch rates have been noted for many years following Tait's (1953) study (Jessen 1956, Hayne 1991). Jones et al (1995) evaluated bias associated with fishing trip length and its effect on confidence intervals, and found that bias significantly affected estimates of catch rates. Ryckman (1983) showed that trip length bias was present in six Michigan creel surveys and that sign of trip length bias was not consistent between surveys.

My current analysis of mean-of-ratios estimator showed that biases associated with fishing trip length and angler party size, and effects of these biases on confidence intervals, were significant. Linear regression analysis showed that catch rates of longer fishing trips tended to be greater, while catch rates tended to decrease with increasing angler party size. Length of trip and angler party size biases existed in both inland and Great Lakes creel surveys, for each of the five angling modes, and for each species of fish. These findings confirm those of Ryckman (1983) and Jones et al (1995), and show that these biases are prevalent throughout Michigan creel surveys. Biases similar to those attributed to the mean-ofratio estimator were not detected for the ratio-ofmeans estimator. Angler party size and length of trip are both accounted for using estimator  $\hat{R}_i$ .

Bias effects associated with mean-of-ratios further magnified by their estimator are inconsistent nature. For example, mean-of-ratios estimator suggests that catch rate of walleye by anglers at Menominee (which boat was underestimated by 20.93%) is only 8.51% greater than at Muskegon (which was overestimated by 84.31%; Table 13). However, catch rate is actually 152.94% greater at Menominee than at Muskegon. Similarly, mean-of-ratios estimator for Chicagon Lake in 1994 (which was overestimated by 7.54%) incorrectly showed a 48.90% reduction from 1993 (which was overestimated by 57.56%), while actual catch rate in 1994 was only 25.09% less. If biases were similar between sites or years, trend information would remain reliable. Consistent biases would characterize long term changes even though estimates for individual time periods or sites are inaccurate. This additional inconsistent variation also confounds an investigator's ability to correctly interpret results of angler catch estimates. Apparent differences or similarities between estimates are masked by these inconsistent biases.

Representative confidence limits are essential to correct interpretation of estimated harvest from creel survey estimates. Biases associated with mean-of-ratios catch rate estimator altered associated confidence limits. These biases were great enough to warrant concern over their interpretation (Cochran 1977).

 $\hat{R}_i$  and  $\overline{R}_i$  actually estimate two different catch rates.  $\hat{R}_i$  estimates total catch per hour while  $\overline{R}_i$  estimates total catch per hour per angler Michigan creel surveys are generally party. designed to collect either complete trip interviews or incomplete trip interviews. Complete trip interviews are collected when a clerk remains at a survey site or area much longer (~8h) than the length of an average trip (~3.5h), thus complete trip interviews are collected with approximate equal probability. Incomplete trip interviews however, are collected when the clerk spends a shorter period of time (<3.5h) at a location. Incomplete trip interviews are collected proportional to trip length - anglers that remain at a location longer are more likely to be interviewed. Results of this study show when  $\overline{R}_i$  is used to estimate  $\hat{R}_i$  two sources of bias are of concern. If catch rates increase with length of trip,  $\overline{R}_i$  will under estimate  $\hat{R}_i$  and if catch rates decrease with length of trip,  $\overline{R}_i$  will over estimate  $\hat{R}_i$ . Similarly, if catch rates increase with angler party size,  $\overline{R}_i$  will under estimate  $\hat{R}_i$  and if catch rates decrease with party size,  $\overline{R}_i$  will over estimate  $\hat{R}_i$ .

Jones et al (1995) showed that when anglers are sampled with equal probability, complete trip interviews,  $\hat{R}_i$  multiplied by an independent estimate of effort produces an unbiased estimate of catch. When anglers are sampled proportional to their trip length (incomplete trip interviews)  $\overline{R}_i$ (calculated per angler - not per angler party) multiplied by an independent estimate of effort produces an unbiased estimate of catch. However, given the current procedure of collecting incomplete-trip interviews by angling party (not by angler), angler party size bias remains a problem.

Estimating sample size necessary for a given level of precision in catch rate provides an investigator with two pieces of information. First, the investigator is able to determine if the chosen precision is in fact attainable at a given level of certainty. Second, the investigator is able to determine how much sampling effort is required to collect the necessary information. Sampling effort (number of interviews collected) is often a function of the number of creel clerks used for a particular survey.

Over sampling results in collecting adequate data at an inflated cost, while under sampling results in collection of expensive inadequate data. Subsampling of anglers from some prior survey at a representative location or time period, will allow the investigator to use the sampling level model developed in this study. Recognizing appropriate sampling effort will help prevent costly mistakes.

#### Recommendations

For Michigan access-site creel surveys utilizing completed-trip interviews, calculate catchper-hour rates using the ratio-of-means estimator  $\hat{R}_i$ . Catch rate information may be collected by angler or angler party since  $\hat{R}_i$  correctly accounts The appropriate formula for for party size. calculating variance of a ratio of means is given by For creel surveys utilizing Cochran (1977). incomplete-trip interviews, catch information should be collected by individual angler. Catchper-hour rates of incomplete-trip interviews are calculated using the mean-of-ratios estimator  $\overline{R}_i$ . Variance of  $\overline{R}_i$  is calculated as for any set of independent samples. These methods correspond with the recommendations of Pollock et al (1994) and are consistent with the findings of Jones et al (1995).

The sampling level model described should prove to be a practical tool for use in designing future creel surveys. From preliminary data collections and historical data sets, appropriate sampling levels for future surveys may be determined for desired catch rate precision. Determination of acceptable sample sizes for largescale creel surveys in particular will allow design of more cost effective surveys.

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Figure 1.–Bias diversity for ratio-of-means and mean-of-ratios estimators at 2, 5, 100, 300, and 500 iterations. Boat angler interviews are from Hagerman Lake walleye fishery.



Figure 2.–Coefficient of variation diversity for ratio-of-means and mean-of-ratios estimators at 2, 5, 100, 300, and 500 iterations. Boat angler interviews are from Hagerman Lake walleye fishery.



Figure 3.–Frequency of absolute value of bias based on under or over estimation of  $\Theta$  by estimator  $\overline{\overline{R}}$ .



Figure 4.–Sample size determination. Sampling quantities (q) vs. angler party catch per hour rates (CPH) and coefficient of variation (CV). Regression coefficients are: ln(q)=7.7168-[ln(CPH)\*0.3659]-[ln(CV)\*1.3701].

Table 1.-List of freshwater fish species evaluated in study.

| Common name     | Scientific name              |
|-----------------|------------------------------|
| Brown trout     | Salmo trutta                 |
| Steelhead       | Oncorhynchus mykiss          |
| Lake trout      | Salvelinus namaycush         |
| Round whitefish | Prosopium cylindraceum       |
| Coho salmon     | Oncorhynchus kisutch         |
| Chinook salmon  | Oncorhynchus tshawytscha     |
| Northern pike   | Esox lucius                  |
| Smallmouth bass | Micropterus dolomieui        |
| Sunfish         | Lepomis gibbosus             |
| Bluegill        | Lepomis macrochirus          |
| Black crappie   | Pomoxis nigromaculatus       |
| Walleye         | Stizostedion vitreum vitreum |
| Yellow perch    | Perca flavescens             |

| Table 2.–Bias attributed to mean-of-ratios estimator ( $\overline{R}$ ) and ratio-of-means estimator ( $\hat{R}$ ). Monte Carlo sampling techniques (500 replications) were used with 90% of the population sampled. Results |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| are from inland black crappie fisheries. Significantly different estimators ( $P_{\alpha}=0.05$ ) and bias (B/ $\sigma$ >0.20) are noted with an '*'                                                                         |
|                                                                                                                                                                                                                              |

|            |     |        | Mean of Ratios |       |                           | Ratio of Means |      |                      |
|------------|-----|--------|----------------|-------|---------------------------|----------------|------|----------------------|
| Mode/Site  | n   | θ      | Bias(%)        | B/σ   | $\overline{\overline{R}}$ | Bias(%)        | B/σ  | $\overline{\hat{R}}$ |
| Boat       |     |        |                |       |                           |                |      |                      |
| Pomeroy    | 58  | 0.2568 | -18.93         | 0.91* | 0.2082*                   | 0.08           | 0.01 | 0.2570               |
| Duck       | 102 | 0.2465 | -5.72          | 0.63* | 0.2324*                   | -0.49          | 0.07 | 0.2477               |
| Open Ice   |     |        |                |       |                           |                |      |                      |
| Fletcher   | 321 | 0.1055 | 41.80          | 0.99* | 0.1496*                   | 0.19           | 0.03 | 0.1057               |
| Ice Shanty |     |        |                |       |                           |                |      |                      |
| Fletcher   | 336 | 0.0610 | 5.08           | 0.46* | 0.0641*                   | 0.00           | 0.00 | 0.0610               |

Table 3.–Bias attributed to mean-of-ratios estimator ( $\overline{R}$ ) and ratio-of-means estimator ( $\hat{R}$ ). Monte Carlo sampling techniques (500 replications) were used with 90% of the population sampled. Results are from inland bluegill fisheries. Significantly different estimators ( $P_{\alpha}$ =0.05) and bias (B/ $\sigma$ >0.20) are noted with an '\*'.

|            |     |        | Mean of Ratios |       |                           | Ratio of Means |            |                      |
|------------|-----|--------|----------------|-------|---------------------------|----------------|------------|----------------------|
| Mode/Site  | n   | θ      | Bias(%)        | B/σ   | $\overline{\overline{R}}$ | Bias(%)        | $B/\sigma$ | $\overline{\hat{R}}$ |
| Boat       |     |        |                |       |                           |                |            |                      |
| Pomeroy    | 58  | 0.0479 | -33.82         | 0.91* | 0.0317*                   | -0.04          | 0.01       | 0.0478               |
| Duck       | 102 | 0.2427 | 39.23          | 0.97* | 0.3379*                   | 0.37           | 0.05       | 0.2436               |
| Open Ice   |     |        |                |       |                           |                |            |                      |
| Fletcher   | 321 | 0.3517 | 25.87          | 0.97* | 0.4427*                   | -0.03          | 0.02       | 0.3514               |
| Ice Shanty |     |        |                |       |                           |                |            |                      |
| Fletcher   | 336 | 0.3030 | 8.91           | 0.86* | 0.3300*                   | -0.03          | 0.01       | 0.3029               |

Table 4.–Bias attributed to mean-of-ratios estimator ( $\overline{R}$ ) and ratio-of-means estimator ( $\hat{R}$ ). Monte Carlo sampling techniques (500 replications) were used with 90% of the population sampled. Results are from Lake Michigan brown trout fisheries. Significantly different estimators ( $P_{\infty}$ =0.05) and bias (B/ $\sigma$ >0.20) are noted with an '\*'.

|                  |       |        | Me      | an of Rati | os                        | Ratio of Means |            |                      |
|------------------|-------|--------|---------|------------|---------------------------|----------------|------------|----------------------|
| Mode/Site        | n     | θ      | Bias(%) | $B/\sigma$ | $\overline{\overline{R}}$ | Bias(%)        | $B/\sigma$ | $\overline{\hat{R}}$ |
| Boat             |       |        |         |            |                           |                |            |                      |
| Stoney Point     | 75    | 0.0662 | 22.96   | 0.85*      | 0.0814*                   | -0.15          | 0.01       | 0.0661               |
| Jutison Point    | 132   | 0.0069 | 5.80    | 0.18       | 0.0073*                   | 1.45           | 0.04       | 0.0070               |
| Cedar River      | 237   | 0.0707 | 16.47   | 0.19       | 0.0823*                   | 0.00           | 0.00       | 0.0707               |
| Yuba Creek       | 319   | 0.0563 | 23.98   | 1.01*      | 0.0698*                   | -0.71          | 0.18       | 0.0559*              |
| Muskegon         | 383   | 0.0087 | 6.90    | 0.27*      | 0.0093*                   | 0.00           | 0.00       | 0.0087               |
| Manistee         | 959   | 0.0489 | 45.40   | 0.99*      | 0.0711*                   | -0.20          | 0.04       | 0.0488               |
| Frankfort        | 1,111 | 0.0199 | 29.15   | 0.86*      | 0.0257*                   | 0.00           | 0.00       | 0.0199               |
| Shore            |       |        |         |            |                           |                |            |                      |
| Jutison Point    | 72    | 0.0177 | 15.82   | 0.63*      | 0.0205*                   | 0.00           | 0.00       | 0.0177               |
| Lighthouse Point | 90    | 0.0285 | 20.00   | 0.64*      | 0.0342*                   | -0.35          | 0.02       | 0.0284               |
| Elk Rapids       | 279   | 0.0235 | 35.32   | 0.93*      | 0.0318*                   | 0.00           | 0.00       | 0.0235               |
| Pier             |       |        |         |            |                           |                |            |                      |
| Menominee        | 79    | 0.0599 | 8.51    | 0.57*      | 0.0650*                   | 0.17           | 0.01       | 0.0600               |
| Jutison Point    | 138   | 0.0671 | -3.13   | 0.31*      | 0.0650*                   | 0.15           | 0.02       | 0.0672               |
| Holland          | 220   | 0.0336 | 14.29   | 0.72*      | 0.0384*                   | 0.60           | 0.09       | 0.0338               |
| Grand Haven      | 302   | 0.0571 | -15.41  | 0.98*      | 0.0483*                   | 0.00           | 0.00       | 0.0571               |
| Ludington        | 437   | 0.0258 | 5.43    | 0.63*      | 0.0272*                   | 0.00           | 0.00       | 0.0258               |
| Manistee         | 668   | 0.0421 | -4.28   | 0.80*      | 0.0403*                   | 0.24           | 0.04       | 0.0422               |

| Table 5.–Bias attributed to mean-of-ratios estimator ( $\overline{R}$ ) and ratio-of-means estimator ( $\hat{R}$ ). Monte |
|---------------------------------------------------------------------------------------------------------------------------|
| Carlo sampling techniques (500 replications) were used with 90% of the population sampled. Results                        |
| are from Lake Michigan chinook salmon fisheries. Significantly different estimators (P <sub>a</sub> =0.05) and bias       |
| $(B/\sigma > 0.20)$ are noted with an '*'.                                                                                |

|                  |       |        | Me      | ean of Rat | tios                      | Ra      | tio of Me | eans                 |
|------------------|-------|--------|---------|------------|---------------------------|---------|-----------|----------------------|
| Mode/Site        | n     | θ      | Bias(%) | B/σ        | $\overline{\overline{R}}$ | Bias(%) | B/σ       | $\overline{\hat{R}}$ |
| Boat             |       |        |         |            |                           |         |           |                      |
| Petoskey         | 73    | 0.0100 | 49.00   | 1.10*      | 0.0149*                   | 0.00    | 0.00      | 0.0100               |
| Escanaba         | 105   | 0.0009 | 44.44   | 0.36*      | 0.0013*                   | 0.00    | 0.00      | 0.0009               |
| Menominee        | 151   | 0.0268 | -11.19  | 0.67*      | 0.0238*                   | 0.00    | 0.00      | 0.0268               |
| Lighthouse Point | 197   | 0.0215 | 6.51    | 0.63*      | 0.0229*                   | -0.01   | 0.04      | 0.0214               |
| Holland          | 330   | 0.0278 | -9.35   | 1.16*      | 0.0252*                   | 0.36    | 0.04      | 0.0279               |
| Ludington        | 1,036 | 0.0206 | -8.68   | 0.94*      | 0.0188*                   | 0.28    | 0.08      | 0.0207               |
| Shore            |       |        |         |            |                           |         |           |                      |
| Bear River       | 52    | 0.0348 | 72.73   | 0.63*      | 0.0601*                   | 0.00    | 0.00      | 0.0348               |
| Elk Rapids       | 80    | 0.0120 | 38.60   | 0.94*      | 0.0166*                   | 0.53    | 0.01      | 0.0121               |
| Jutison Point    | 258   | 0.0160 | -7.50   | 0.54*      | 0.0148*                   | 0.00    | 0.00      | 0.0160               |
| Pier             |       |        |         |            |                           |         |           |                      |
| Frankfort        | 121   | 0.0191 | -20.94  | 0.89*      | 0.0151*                   | -0.52   | 0.04      | 0.0190               |
| South Haven      | 167   | 0.0026 | 50.00   | 0.58*      | 0.0039*                   | 0.00    | 0.00      | 0.0026               |
| Manistee         | 185   | 0.0019 | 94.74   | 0.80*      | 0.0037*                   | 0.00    | 0.00      | 0.0019               |
| Holland          | 220   | 0.0053 | -35.85  | 0.85*      | 0.0034*                   | 0.00    | 0.00      | 0.0053               |
| Benton Harbor    | 328   | 0.0035 | -31.43  | 0.49*      | 0.0024*                   | 0.00    | 0.00      | 0.0035               |

Table 6.–Bias attributed to mean-of-ratios estimator ( $\overline{R}$ ) and ratio-of-means estimator ( $\hat{R}$ ). Monte Carlo sampling techniques (500 replications) were used with 90% of the population sampled. Results are from Lake Michigan coho salmon fisheries. Significantly different estimators ( $P_{\infty}$ =0.05) and bias (B/ $\sigma$ >0.20) are noted with an '\*'.

|               |       |        | Me      | an of Rati | os                        | Ratio of Means |      |                      |
|---------------|-------|--------|---------|------------|---------------------------|----------------|------|----------------------|
| Mode/Site     | n     | θ      | Bias(%) | B/σ        | $\overline{\overline{R}}$ | Bias(%)        | B/σ  | $\overline{\hat{R}}$ |
| Boat          |       |        |         |            |                           |                |      |                      |
| Portage       | 114   | 0.0252 | -7.14   | 0.80*      | 0.0234*                   | 0.00           | 0.00 | 0.0252               |
| Benton Harbor | 165   | 0.0348 | 30.46   | 0.95*      | 0.0454*                   | -0.29          | 0.04 | 0.0347               |
| New Buffalo   | 203   | 0.0586 | 50.85   | 0.95*      | 0.0884*                   | -0.68          | 0.09 | 0.0582               |
| Manistee      | 385   | 0.0086 | -15.12  | 0.58*      | 0.0073*                   | 0.00           | 0.00 | 0.0086               |
| Ludington     | 894   | 0.0056 | -8.93   | 0.56*      | 0.0051*                   | 0.00           | 0.00 | 0.0056               |
| South Haven   | 1,148 | 0.0020 | 45.00   | 1.01*      | 0.0029*                   | 0.00           | 0.00 | 0.0020               |
| Shore         |       |        |         |            |                           |                |      |                      |
| Bear River    | 52    | 0.0087 | 63.22   | 0.82*      | 0.0142*                   | 1.15           | 0.04 | 0.0088               |
| Pier          |       |        |         |            |                           |                |      |                      |
| Grand Haven   | 105   | 0.0022 | 77.27   | 0.76*      | 0.0039*                   | 0.00           | 0.00 | 0.0022               |
| South Haven   | 167   | 0.0337 | -31.16  | 0.94*      | 0.0232*                   | 0.30           | 0.02 | 0.0338               |
| Frankfort     | 194   | 0.0065 | 66.15   | 0.96*      | 0.0108*                   | 1.54           | 0.09 | 0.0064               |
| Benton Harbor | 328   | 0.1131 | 33.16   | 0.99*      | 0.1506*                   | -0.09          | 0.02 | 0.1130               |
| Grand Haven   | 492   | 0.0035 | 2.86    | 0.11       | 0.0036*                   | 0.00           | 0.00 | 0.0035               |

Table 7.–Bias attributed to mean-of-ratios estimator ( $\overline{R}$ ) and ratio-of-means estimator ( $\hat{R}$ ). Monte Carlo sampling techniques (500 replications) were used with 90% of the population sampled. Results are from Lake Michigan lake trout fisheries. Significantly different estimators ( $P_{\infty}$ =0.05) and bias (B/ $\sigma$ >0.20) are noted with an '\*'.

|               |       |        | Mea     | an of Rati | os                        | Ratio of Means |            |                      |
|---------------|-------|--------|---------|------------|---------------------------|----------------|------------|----------------------|
| Mode/Site     | n     | θ      | Bias(%) | B/σ        | $\overline{\overline{R}}$ | Bias(%)        | $B/\sigma$ | $\overline{\hat{R}}$ |
| Boat          |       |        |         |            |                           |                |            |                      |
| Benton Harbor | 167   | 0.0166 | 20.48   | 0.76*      | 0.0132*                   | 0.60           | 0.04       | 0.0165               |
| Petoskey      | 200   | 0.0958 | 27.66   | 0.99*      | 0.1223*                   | -0.21          | 0.04       | 0.0956               |
| Holland       | 307   | 0.0490 | -10.20  | 1.12*      | 0.0440*                   | 0.00           | 0.00       | 0.0490               |
| Manistee      | 535   | 0.0142 | -28.87  | 0.92*      | 0.0101*                   | 0.00           | 0.00       | 0.0142               |
| South Haven   | 816   | 0.0194 | -4.64   | 0.40*      | 0.0185*                   | 0.00           | 0.00       | 0.0194               |
| Frankfort     | 1,111 | 0.0278 | 1.80    | 0.14       | 0.0283*                   | 0.00           | 0.00       | 0.0278               |

Table 8.–Bias attributed to mean-of-ratios estimator ( $\overline{R}$ ) and ratio-of-means estimator ( $\hat{R}$ ). Monte Carlo sampling techniques (500 replications) were used with 90% of the population sampled. Results are from Inland northern pike fisheries. Significantly different estimators ( $P_{\infty}$ =0.05) and bias (B/ $\sigma$ >0.20) are noted with an '\*'.

|            |     |        | Me      | an of Rati | os                        | Ratio of Means |      |                      |
|------------|-----|--------|---------|------------|---------------------------|----------------|------|----------------------|
| Mode/Site  | n   | θ      | Bias(%) | B/σ        | $\overline{\overline{R}}$ | Bias(%)        | B/σ  | $\overline{\hat{R}}$ |
| Open Ice   |     |        |         |            |                           |                |      |                      |
| Fletcher   | 321 | 0.0219 | -2.74   | 0.27*      | 0.0213*                   | 0.00           | 0.00 | 0.0219               |
| Ice Shanty |     |        |         |            |                           |                |      |                      |
| Fletcher   | 336 | 0.0188 | 25.00   | 1.05*      | 0.0235*                   | 0.00           | 0.00 | 0.0188               |

Table 9.–Bias attributed to mean-of-ratios estimator ( $\overline{R}$ ) and ratio-of-means estimator ( $\hat{R}$ ). Monte Carlo sampling techniques (500 replications) were used with 90% of the population sampled. Results are from Lake Michigan round whitefish fisheries. Significantly different estimators (P<sub>ex</sub>=0.05) and bias (B/ $\sigma$ >0.20) are noted with an '\*'.

| Mode/Site    |     |        | Me      | an of Rati | OS                        | Ratio of Means |      |                      |
|--------------|-----|--------|---------|------------|---------------------------|----------------|------|----------------------|
|              | n   | θ      | Bias(%) | $B/\sigma$ | $\overline{\overline{R}}$ | Bias(%)        | B/σ  | $\overline{\hat{R}}$ |
| Boat         |     |        |         |            |                           |                |      |                      |
| Portage Lake | 137 | 0.0025 | 68.00   | 0.76*      | 0.0042*                   | 0.00           | 0.00 | 0.0025               |
| Ludington    | 218 | 0.0049 | 40.82   | 0.89*      | 0.0069*                   | 0.00           | 0.00 | 0.0049               |
| Elk Rapids   | 319 | 0.0100 | 15.00   | 0.67*      | 0.0115*                   | 0.00           | 0.00 | 0.0100               |
| Pier         |     |        |         |            |                           |                |      |                      |
| Ludington    | 81  | 0.0193 | -73.06  | 1.05*      | 0.0052*                   | -2.59          | 0.07 | 0.0188               |
| Frankfort    | 136 | 0.0088 | -80.68  | 1.06*      | 0.0017*                   | -1.14          | 0.04 | 0.0087               |
| Manistee     | 185 | 0.0624 | -1.44   | 0.13       | 0.0615*                   | 0.48           | 0.04 | 0.0627               |

Table 10.–Bias attributed to mean-of-ratios estimator ( $\overline{R}$ ) and ratio-of-means estimator ( $\hat{R}$ ). Monte Carlo sampling techniques (500 replications) were used with 90% of the population sampled. Results are from Lake Michigan smallmouth bass fisheries. Significantly different estimators ( $P_{\infty}$ =0.05) and bias (B/ $\sigma$ >0.20) are noted with an '\*'.

|                            |     |        | Me      | an of Rati | os                        | Ratio of Means |      |                      |
|----------------------------|-----|--------|---------|------------|---------------------------|----------------|------|----------------------|
| Mode/Site                  | n   | θ      | Bias(%) | B/σ        | $\overline{\overline{R}}$ | Bias(%)        | B/σ  | $\overline{\hat{R}}$ |
| Boat                       |     |        |         |            |                           |                |      |                      |
| Jutison Point              | 84  | 0.0209 | 29.19   | 0.91*      | 0.0270*                   | -0.48          | 0.04 | 0.0208               |
| Escanaba                   | 103 | 0.0011 | -27.27  | 0.27*      | 0.0008*                   | 0.00           | 0.00 | 0.0011               |
| Old Coast<br>Guard Station | 163 | 0.0032 | 78.12   | 1.12*      | 0.0057*                   | 0.00           | 0.00 | 0.0032               |
| Cedar River                | 187 | 0.0255 | -29.41  | 1.12*      | 0.0180*                   | -0.39          | 0.04 | 0.0254               |
| Frankfort                  | 538 | 0.0003 | 100.00  | 0.27*      | 0.0006*                   | 0.00           | 0.00 | 0.0003               |
| Shore                      |     |        |         |            |                           |                |      |                      |
| Cedar River                | 54  | 0.0429 | -62.00  | 0.99*      | 0.0163*                   | -0.70          | 0.03 | 0.0426               |
| Elk Rapids                 | 110 | 0.0395 | 17.22   | 0.76*      | 0.0463*                   | -0.51          | 0.04 | 0.0393               |
| Jutison Point              | 397 | 0.0041 | 41.46   | 0.76*      | 0.0058*                   | 2.44           | 0.09 | 0.0042               |
| Pier                       |     |        |         |            |                           |                |      |                      |
| Manistee                   | 76  | 0.0030 | -43.33  | 0.58*      | 0.0017*                   | 3.33           | 0.09 | 0.0031               |
| Grand Haven                | 95  | 0.0042 | -30.95  | 0.58*      | 0.0029*                   | 0.00           | 0.00 | 0.0042               |
| Holland                    | 102 | 0.0082 | 6.10    | 0.22*      | 0.0087*                   | -2.44          | 0.09 | 0.0080               |

|                  |       |        | Me      | an of Ratio | OS                        | Ratio of Means |      |                      |
|------------------|-------|--------|---------|-------------|---------------------------|----------------|------|----------------------|
| Mode/Site        | n     | θ      | Bias(%) | B/σ         | $\overline{\overline{R}}$ | Bias(%)        | B/σ  | $\overline{\hat{R}}$ |
| Boat             |       |        |         |             |                           |                |      |                      |
| Old Coast        |       |        |         |             |                           |                |      |                      |
| Guard Station    | 82    | 0.0045 | -8.89   | 0.36*       | 0.0041*                   | 0.00           | 0.00 | 0.0045               |
| New Buffalo      | 145   | 0.0164 | 17.68   | 0.65*       | 0.0193*                   | 0.00           | 0.00 | 0.0164               |
| Portage Lake     | 178   | 0.0207 | 14.01   | 0.65*       | 0.0236*                   | -0.48          | 0.04 | 0.0206               |
| Grand Haven      | 194   | 0.0148 | 10.14   | 0.67*       | 0.0163*                   | 0.00           | 0.00 | 0.0148               |
| Holland          | 330   | 0.0214 | -15.42  | 0.74*       | 0.0181*                   | 0.00           | 0.00 | 0.0214               |
| Manistee         | 959   | 0.0179 | -37.43  | 1.00*       | 0.0112*                   | 0.00           | 0.00 | 0.0179               |
| Frankfort        | 1,111 | 0.0320 | -13.44  | 0.96*       | 0.0277*                   | 0.00           | 0.00 | 0.0320               |
| Shore            |       |        |         |             |                           |                |      |                      |
| Yuba Creek       | 51    | 0.0952 | 1.47    | 0.13        | 0.0966*                   | 0.11           | 0.01 | 0.0953               |
| Lighthouse Point | 90    | 0.0665 | 5.71    | 0.57*       | 0.0703*                   | 0.00           | 0.00 | 0.0665               |
| Elk Rapids       | 279   | 0.0242 | 19.42   | 1.05*       | 0.0289*                   | 0.00           | 0.00 | 0.0242               |
| Jutison Point    | 334   | 0.0073 | 73.97   | 0.80*       | 0.0127*                   | 0.00           | 0.00 | 0.0073               |
| Pier             |       |        |         |             |                           |                |      |                      |
| Muskegon         | 73    | 0.0114 | -21.93  | 1.12*       | 0.0089*                   | -0.88          | 0.04 | 0.0113               |
| South Haven      | 212   | 0.0033 | -36.36  | 0.54*       | 0.0021*                   | 0.00           | 0.00 | 0.0033               |
| Grand Haven      | 302   | 0.0069 | -4.35   | 0.27*       | 0.0066*                   | 0.00           | 0.00 | 0.0069               |
| Manistee         | 422   | 0.0045 | -26.67  | 0.54*       | 0.0033*                   | 0.00           | 0.00 | 0.0045               |
| Benton Harbor    | 713   | 0.0197 | -2.03   | 0.18        | 0.0193*                   | 0.00           | 0.00 | 0.0197               |

Table 11.–Bias attributed to mean-of-ratios estimator ( $\overline{R}$ ) and ratio-of-means estimator ( $\hat{R}$ ). Monte Carlo sampling techniques (500 replications) were used with 90% of the population sampled. Results are from Lake Michigan steelhead fisheries. Significantly different estimators ( $P_{\infty}$ =0.05) and bias (B/ $\sigma$ >0.20) are noted with an '\*'.

Table 12.–Bias attributed to mean-of-ratios estimator ( $\overline{R}$ ) and ratio-of-means estimator ( $\hat{R}$ ). Monte Carlo sampling techniques (500 replications) were used with 90% of the population sampled. Results are from inland sunfish spp fisheries. Significantly different estimators ( $P_{\infty}$ =0.05) and bias (B/ $\sigma$ >0.20) are noted with an '\*'.

|            |     |        | Mea     | an of Rati | os                        | Ra      | tio of Me | ans                  |
|------------|-----|--------|---------|------------|---------------------------|---------|-----------|----------------------|
| Mode/Site  | n   | θ      | Bias(%) | B/σ        | $\overline{\overline{R}}$ | Bias(%) | B/σ       | $\overline{\hat{R}}$ |
| Boat       |     |        |         |            |                           |         |           |                      |
| Duck       | 102 | 0.1118 | 72.99   | 0.89*      | 0.1934*                   | -0.54   | 0.04      | 0.1112               |
| Open Ice   |     |        |         |            |                           |         |           |                      |
| Fletcher   | 321 | 0.0403 | 83.13   | 1.00*      | 0.0738*                   | 0.00    | 0.00      | 0.0403               |
| Ice Shanty |     |        |         |            |                           |         |           |                      |
| Fletcher   | 336 | 0.0412 | 24.51   | 0.90*      | 0.0513*                   | 0.24    | 0.02      | 0.0413               |

|                 |       |        | Me      | an of Rati | os                        | Ra      | tio of Me  | ans                  |
|-----------------|-------|--------|---------|------------|---------------------------|---------|------------|----------------------|
| Mode/Site       | n     | θ      | Bias(%) | $B/\sigma$ | $\overline{\overline{R}}$ | Bias(%) | $B/\sigma$ | $\overline{\hat{R}}$ |
|                 |       |        | Inl     | and        |                           |         |            |                      |
| Boat            |       |        |         |            |                           |         |            |                      |
| Pomeroy         | 58    | 0.0413 | 29.06   | 0.89*      | 0.0533*                   | -0.48   | 0.04       | 0.0411               |
| Hagerman        | 202   | 0.1330 | -15.79  | 0.94*      | 0.1120*                   | -0.08   | 0.01       | 0.1329               |
| Stanley         | 328   | 0.0205 | 11.22   | 1.03*      | 0.0228*                   | 0.00    | 0.00       | 0.0205               |
| Chicagon (1993) | 598   | 0.0549 | 57.56   | 1.01*      | 0.0865*                   | 0.18    | 0.04       | 0.0550               |
| Chicagon (1994) | 801   | 0.0411 | 7.54    | 0.69*      | 0.0442*                   | 0.24    | 0.04       | 0.0412               |
| Burt            | 1,044 | 0.1254 | 12.84   | 1.03*      | 0.1415*                   | -0.08   | 0.04       | 0.1253               |
| Open Ice        |       |        |         |            |                           |         |            |                      |
| Chicagon (1993) | 58    | 0.0233 | 45.92   | 0.96*      | 0.0340*                   | 0.00    | 0.00       | 0.0233               |
|                 |       |        | Lake M  | ſichigan   |                           |         |            |                      |
| Boat            |       |        |         |            |                           |         |            |                      |
| Menominee       | 51    | 0.0129 | -20.93  | 0.60*      | 0.0102*                   | 0.00    | 0.00       | 0.0129               |
| Muskegon        | 120   | 0.0051 | 84.31   | 0.96*      | 0.0094*                   | 1.96    | 0.04       | 0.0052               |
| Tacoosh River   | 225   | 0.1350 | 4.37    | 0.53*      | 0.1409*                   | 0.15    | 0.03       | 0.1352               |
| Jutison Point   | 305   | 0.2029 | 10.55   | 0.96*      | 0.2243*                   | 0.10    | 0.04       | 0.2031               |
| Escanaba        | 528   | 0.1205 | 1.24    | 0.34*      | 0.1220*                   | 0.00    | 0.00       | 0.1205               |
| Shore           |       |        |         |            |                           |         |            |                      |
| Cedar River     | 95    | 0.0271 | -19.56  | 0.79*      | 0.0218*                   | 0.00    | 0.00       | 0.0271               |
| Jutison Point   | 535   | 0.0714 | 21.43   | 0.98*      | 0.0867*                   | 0.00    | 0.00       | 0.0714               |
| Pier            |       |        |         |            |                           |         |            |                      |
| Holland         | 131   | 0.0155 | -0.65   | 0.04       | 0.0154                    | 0.65    | 0.04       | 0.0156               |
| Menominee       | 190   | 0.0072 | 18.06   | 0.58*      | 0.0085*                   | 0.00    | 0.00       | 0.0072               |
| Jutison Point   | 282   | 0.0054 | 22.22   | 0.54*      | 0.0066*                   | -1.85   | 0.09       | 0.0053               |

Table 13.–Bias attributed to mean-of-ratios estimator ( $\overline{R}$ ) and ratio-of-means estimator ( $\hat{R}$ ). Monte Carlo sampling techniques (500 replications) were used with 90% of the population sampled. Results are from walleye fisheries. Significantly different estimators (P<sub>ex</sub>=0.05) and bias (B/ $\sigma$ >0.20) are noted with an '\*'.

Table 14.–Bias attributed to mean-of-ratios estimator ( $\overline{R}$ ) and ratio-of-means estimator ( $\hat{R}$ ). Monte Carlo sampling techniques (500 replications) were used with 90% of the population sampled. Results are from yellow perch fisheries. Significantly different estimators ( $P_{\infty}$ =0.05) and bias (B/ $\sigma$ >0.20) are noted with an '\*'.

|                 |       |        | Me      | an of Rati | os                        | R       | atio of Me | ans                  |
|-----------------|-------|--------|---------|------------|---------------------------|---------|------------|----------------------|
| Mode/Site       | n     | θ      | Bias(%) | B/σ        | $\overline{\overline{R}}$ | Bias(%) | $B/\sigma$ | $\overline{\hat{R}}$ |
|                 |       |        | Inl     | and        |                           |         |            |                      |
| Boat            |       |        |         |            |                           |         |            |                      |
| Stanley         | 328   | 0.3893 | 2.31    | 0.45*      | 0.3983*                   | 0.10    | 0.02       | 0.3897               |
| Chicagon (1993) | 598   | 0.2785 | 6.28    | 0.87*      | 0.2960*                   | 0.14    | 0.04       | 0.2789               |
| Chicagon (1994) | 801   | 0.2607 | 24.86   | 1.00*      | 0.3255*                   | -0.04   | 0.01       | 0.2608               |
| Open Ice        |       |        |         |            |                           |         |            |                      |
| Chicagon (1993) | 58    | 0.5404 | -9.70   | 0.78*      | 0.4880*                   | -0.48   | 0.07       | 0.5378               |
| Fletcher        | 321   | 0.2731 | 11.83   | 0.96*      | 0.3054*                   | -0.11   | 0.03       | 0.2728               |
| Ice Shanty      |       |        |         |            |                           |         |            |                      |
| Fletcher        | 336   | 0.2914 | 19.11   | 0.96*      | 0.3471*                   | 0.00    | 0.00       | 0.2914               |
|                 |       |        | Lake M  | Iichigan   |                           |         |            |                      |
| Boat            |       |        |         |            |                           |         |            |                      |
| Menominee       | 89    | 0.0200 | 285.50  | 0.95*      | 0.0771*                   | 1.00    | 0.04       | 0.0202               |
| Cedar River     | 134   | 0.6871 | 33.30   | 0.97*      | 0.9159*                   | -0.29   | 0.04       | 0.6851               |
| Tacoosh River   | 225   | 0.0194 | 87.11   | 0.94*      | 0.0363*                   | -0.52   | 0.04       | 0.0193               |
| Yuba Creek      | 319   | 0.0703 | 27.88   | 0.88*      | 0.0899*                   | 0.14    | 0.01       | 0.0704               |
| Escanaba        | 647   | 0.0986 | 1.72    | 0.25*      | 0.1003*                   | 0.30    | 0.07       | 0.0989               |
| Ludington       | 853   | 0.2486 | 34.63   | 0.99*      | 0.3347*                   | -0.08   | 0.02       | 0.2484               |
| South Haven     | 1,148 | 4.3892 | 17.18   | 0.99*      | 5.1432*                   | 0.01    | 0.01       | 4.3898               |
| Shore           |       |        |         |            |                           |         |            |                      |
| Elk Rapids      | 115   | 0.1002 | 52.20   | 0.90*      | 0.1525*                   | 0.00    | 0.00       | 0.1002               |
| Jutison Point   | 138   | 0.0120 | -27.50  | 0.74*      | 0.0087*                   | 0.00    | 0.00       | 0.0120               |
| Pier            |       |        |         |            |                           |         |            |                      |
| Muskegon        | 50    | 0.4630 | -15.94  | 0.87*      | 0.3892*                   | 0.28    | 0.03       | 0.4643               |
| Menominee       | 169   | 1.1192 | -7.46   | 0.85*      | 1.0357*                   | 0.33    | 0.06       | 1.1229               |
| Jutison Point   | 243   | 0.6372 | -0.36   | 0.09       | 0.6349*                   | 0.14    | 0.03       | 0.6381               |
| Manistee        | 422   | 0.0185 | -5.95   | 0.49*      | 0.0174*                   | 1.08    | 0.09       | 0.0187               |
| Holland         | 669   | 0.6684 | -14.51  | 0.96*      | 0.5714*                   | -0.01   | < 0.01     | 0.6683               |
| Grand Haven     | 906   | 0.8632 | -1.09   | 0.28*      | 0.8538*                   | -0.20   | 0.06       | 0.8615               |

|                 |                 |          |           |         | Slope   |  |  |
|-----------------|-----------------|----------|-----------|---------|---------|--|--|
| Mode/Site       | Species         | n        | Intercept | Hours   | Anglers |  |  |
|                 |                 | Inlan    | d         |         |         |  |  |
| Boat            |                 |          |           |         |         |  |  |
| Chicagon (1993) | Walleye         | 598      | 0.2163    | ns      | -0.0615 |  |  |
| Chicagon (1994) | Walleye         | 801      | 0.0744    | ns      | -0.0146 |  |  |
| Burt            | Walleye         | 1,044    | 0.2589    | ns      | -0.0547 |  |  |
| Chicagon (1994) | Yellow Perch    | 801      | 0.4553    | -0.0388 | ns      |  |  |
| Pomeroy         | Black Crappie   | 58       | -0.3406   | 0.1435  | ns      |  |  |
| Ice Shanty      |                 |          |           |         |         |  |  |
| Fletcher        | Northern Pike   | 336      | 0.0572    | ns      | -0.0182 |  |  |
|                 |                 | Lake Mic | higan     |         |         |  |  |
| Boat            |                 |          |           |         |         |  |  |
| Petoskey        | Lake Trout      | 200      | 0.2374    | ns      | -0.0529 |  |  |
| Holland         | Lake Trout      | 307      | 0.0108    | 0.0072  | ns      |  |  |
| Manistee        | Lake Trout      | 535      | -0.0054   | 0.0018  | 0.0033  |  |  |
| New Buffalo     | Coho            | 203      | 0.2398    | -0.0337 | ns      |  |  |
| Manistee        | Coho            | 385      | 0.0015    | 0.0031  | -0.0038 |  |  |
| Ludington       | Coho            | 894      | 0.0005    | 0.0010  | ns      |  |  |
| South Haven     | Coho            | 1,148    | 0.0087    | -0.0012 | ns      |  |  |
| Petoskey        | Chinook         | 73       | 0.0584    | ns      | -0.0198 |  |  |
| Menominee       | Chinook         | 151      | 0.0020    | 0.0041  | ns      |  |  |
| Holland         | Chinook         | 330      | 0.0070    | 0.0040  | ns      |  |  |
| Ludington       | Chinook         | 1,036    | 0.0139    | 0.0035  | -0.0050 |  |  |
| Yuba Creek      | Brown Trout     | 319      | 0.1284    | -0.0144 | ns      |  |  |
| Manistee        | Brown Trout     | 959      | 0.1625    | ns      | -0.0423 |  |  |
| Frankfort       | Brown Trout     | 1,111    | 0.0624    | -0.0030 | -0.0087 |  |  |
| Menominee       | Yellow Perch    | 89       | 0.4001    | ns      | -0.1204 |  |  |
| Cedar River     | Yellow Perch    | 134      | 2.4827    | ns      | -0.6438 |  |  |
| Yuba Creek      | Yellow Perch    | 319      | 0.1705    | 0.0456  | -0.1300 |  |  |
| Ludington       | Yellow Perch    | 853      | 0.7940    | ns      | -0.1989 |  |  |
| South Haven     | Yellow Perch    | 1,148    | 10.2242   | -0.4891 | -1.1236 |  |  |
| Jutison Point   | Walleye         | 305      | 0.3349    | 0.0235  | -0.0872 |  |  |
| Escanaba        | Walleye         | 528      | 0.1547    | 0.0110  | -0.0379 |  |  |
| Holland         | Steelhead       | 330      | 0.0014    | 0.0037  | ns      |  |  |
| Manistee        | Steelhead       | 959      | -0.0139   | 0.0059  | ns      |  |  |
| Frankfort       | Steelhead       | 1,111    | -0.0048   | 0.0065  | ns      |  |  |
| Cedar River     | Smallmouth Bass | 187      | -0.0001   | 0.0059  | ns      |  |  |

Table 15.–Significant ( $P_{\alpha}$ =0.05) stepwise regression coefficients from boat and ice shanty interviews. Non-significant coefficients are noted as "ns".

|               |                 |          |           | Slope   |         |  |
|---------------|-----------------|----------|-----------|---------|---------|--|
| Mode/Site     | Species         | n        | Intercept | Hours   | Anglers |  |
|               |                 | Inlan    | nd        |         |         |  |
| Open Ice      |                 |          |           |         |         |  |
| Fletcher      | Bluegill        | 321      | 0.8413    | ns      | -0.1977 |  |
| Fletcher      | Sunfish         | 321      | 0.2185    | ns      | -0.0721 |  |
| Fletcher      | Black Crappie   | 321      | 0.3667    | ns      | -0.1082 |  |
|               |                 | Lake Mic | chigan    |         |         |  |
| Shore         |                 |          |           |         |         |  |
| Cedar River   | Walleye         | 95       | -0.0156   | 0.0219  | ns      |  |
| Jutison Point | Walleye         | 535      | 0.1409    | ns      | -0.0319 |  |
| Cedar River   | Smallmouth Bass | 54       | -0.0528   | 0.0395  | ns      |  |
| Pier          |                 |          |           |         |         |  |
| Benton Harbor | Coho            | 328      | 0.2290    | -0.0253 | ns      |  |
| Jutison Point | Brown Trout     | 138      | -0.0011   | 0.0233  | ns      |  |
| Menominee     | Yellow Perch    | 169      | -0.0282   | 0.4914  | ns      |  |
| Holland       | Yellow Perch    | 669      | 0.0542    | 0.2665  | ns      |  |
| Grand Haven   | Yellow Perch    | 906      | 0.9072    | 0.1292  | -0.3024 |  |
| Muskegon      | Steelhead       | 73       | -0.0102   | 0.0068  | ns      |  |
| Manistee      | Steelhead       | 422      | -0.0012   | 0.0015  | ns      |  |
| Ludington     | Round Whitefish | 81       | -0.0319   | 0.0153  | ns      |  |
| Frankfort     | Round Whitefish | 136      | -0.0060   | 0.0026  | ns      |  |
| Manistee      | Round Whitefish | 185      | 0.0685    | 0.0297  | -0.0606 |  |

Table 16.–Significant ( $P_{\infty}$ =0.05) stepwise regression coefficients from open ice, shore and pier angler interviews. Non-significant coefficients are noted as "ns".

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Report approved by Richard D. Clark Jr. Alan D. Sutton, Graphics Kathryn L. Champagne, DTP